



# Effects of Vertical Component of Earthquakes on Cable-Stayed Bridges

**Behnam Babaei Ravandi and Shervin Maleki\****Department of Civil Engineering, Sharif University of Technology, Tehran, Iran*

**\*Corresponding author:** Shervin Maleki, Department of Civil Engineering, Sharif University of Technology, Tehran, Iran.

**Received Date:** November 02, 2021

**Published Date:** January 03, 2022

## Abstract

The vertical component of ground motions is known to cause severe damages to certain structures. Long span cable-stayed bridges are among those vulnerable structures due to their high mass and cables that take no compression. In this paper, the vertical earthquake effects on several cable-stayed bridges have been investigated using 3-D nonlinear time history finite element analyses. Different main span lengths, pylon shapes and pylon/deck connection types are considered. The results indicate that the vertical ground motion component should be considered in the analysis of such bridges and affects many key elements of the bridge.

## Introduction

The first cable stayed bridge was built in the mid twentieth century. Since then, the construction of cable-stayed bridges has spread rapidly and nowadays this type of bridge is one of the most used bridge types for long span lengths. Cable-stayed bridges are popular both from structural aspects and aesthetic point of view.

Seismic evaluation of bridges has been the subject of research for many years. However, the effect of vertical component of an earthquake has been researched only for few types of bridges. The vertical component of ground motions near an active fault has been known to be high and have caused severe damages to certain structures vulnerable to vertical acceleration. Long span bridges like cable-stayed bridges are very massive and are only supported on the pylons. These structures can be vulnerable to vertical acceleration even when they are built away from active faults. There is a need for such an investigation into the behavior of cable-stayed bridges subjected to vertical ground motion simultaneously with horizontal ground motions.

To the best knowledge of the authors, the effects of vertical component of an earthquake on cable-stayed bridges in the form presented here has not been investigated before. To achieve an

accurate estimate of the vertical component effects, different main span lengths, pylon shapes and pylon/deck connection types were considered. The results of 3-D nonlinear time history finite element analyses of such cable-stayed bridges subjected to three components of earthquakes were compared with analyses under only horizontal components. The results indicated that the vertical ground motion component should be considered in the analysis of cable-stayed bridges and greatly affects the deck and pylon internal forces.

## Literature Review

The first complete analytical study into the effect of vertical ground motions on ordinary bridges was conducted by Saadeghvaziri & Foutch [1]. They used a finite element code capable of modeling the inelastic behavior of reinforced concrete columns under combined horizontal and vertical deformations. With three-dimensional finite-element models of eight bridges, they showed that the vertical acceleration causes varying axial forces in the piers and a pinched hysteresis loop in the columns.

Yu et al. [2] showed that vertical accelerations could significantly increase the tensile stresses in the deck and in axial forces (about

20%) while only a marginal change in the longitudinal moment was observed. Button et al. [3] worked on parametric studies of the vertical ground motion effect, including ground motion and structural characteristic of bridges. Gloyd [4] studied values for vertical deck shear and bending moment for two continuous span bridges and showed that the dynamic response from vertical acceleration can be much larger than the dead load effects and a reversal of flexure in the deck can occur in both positive and negative moment areas. Elnashai & Papazoglou [5] and Collier & Elnashai [6] focused on near-fault ground motion studies. They proposed that the damping ratios for elements which are susceptible to vertical excitation should be limited to 2%. They concluded that the moments and axial forces in piers fluctuate from null up to twice the dead load; moreover, they asserted that heavier decks intensify the vertical effects of ground motions.

More recently, Veletzos et al. [7] investigated the effect of vertical compound of ground motion on the seismic response of precast segmental concrete bridges. They found 400% increase in bending rotations due to vertical ground motion.

Abdel-Ghaffar & Nazmy [8] investigated nonlinear seismic behavior of cable-stayed bridges. They showed that for long span cable-stayed bridges nonlinear dynamic analysis is a necessity. Shrestha [9] considered responses of cable-stayed bridges subjected to earthquakes with and without vertical ground motion using near fault ground motions.

### Bridge Characteristics

In this study, the most typical features of commonly constructed

cable-stayed bridges were identified and used in the numerical studies of this research. More than 45 cable-stayed bridges were categorized based on parameters like span length, pylon shape, deck to pylon connection type. The main features of the finite element (FE) models were as follows.

### Span lengths

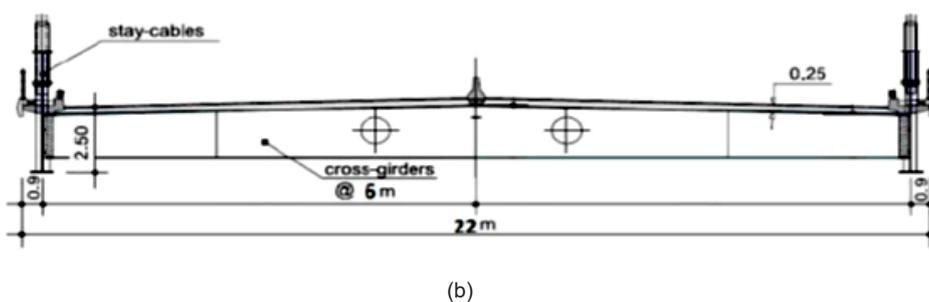
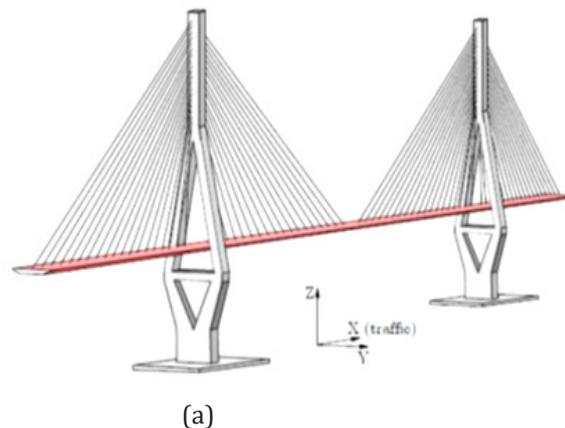
Investigation shows that most of the cable-stayed bridges constructed and in use have more than two spans. As a result, all the bridges analyzed in this study had three spans with two pylons. The variation in middle span length for cable-stayed bridges analyzed were chosen to be 300 meters, 400 meters and 500 meters long. The lengths of the side-spans, pylon height and the number of stay cables were determined based on a commonly used (rule-of-thumb) fraction of the main span length. The side-span lengths were considered as 40% of the main span length. The height from the deck to top of the pylons were considered as 30% of the main span length. In addition, the clear height of the pylon below the deck was assumed to be 50 meters for all models.

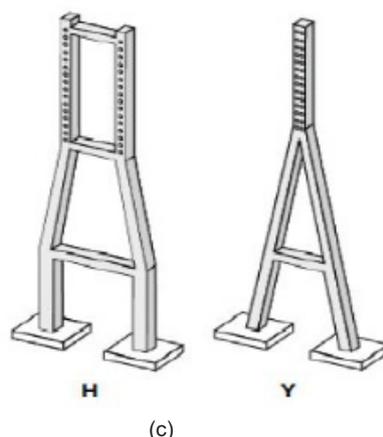
### Cables

Cables were arranged as semi-fan for all bridges. The horizontal distances between cables' attachment points to the deck were 10 meters for the main and 8 meters for the side spans.

### Pylon shapes

'H' and 'inverted Y' pylon shapes were chosen since they are mostly used shapes and typically preferred by designers (see Figure 1).





**Figure 1:** Typical bridge model components; (a) Model with 3 spans and inverted Y pylon, (b) bridge superstructure cross-section, (c) pylon types: H and inverted Y.

### Deck-Pylon connection

Two types of connection were selected for this study. In the first type, the deck was connected only in the horizontal directions to the pylon and the weight of the bridge was supported by cables. In the second type, the deck was connected to the pylons in the vertical and transverse directions with an elastomeric bearing and the longitudinal direction was released. Both connections restricted rotations of the deck in the longitudinal direction.

Table 1 provides a convenient summary of the geometric characteristic of all bridge models. According to Table 1, there are 12 main models for parametric study. Moreover, there is another model in which the pylons stiffness and mass are reduced by 50% to determine the effect of changing the stiffness of pylons on cable-stayed bridges responses. Table 2 provides some key vertical and horizontal dynamic characteristic of the bridge models.

**Table 1:** Bridge models geometric characteristics.

Bridge Model	Span length (m)	Pylon type	Vertical Deck-Pylon Connection	Pylon height (m)	Side span length (m)	Bridge length (m)	Base of Pylon Size (m)
Y300	300	inverted Y	Released	140	120	540	5 × 6
Y300E	300	inverted Y	Elastomeric	140	120	540	5 × 6
H300	300	H	Released	140	120	540	7 × 7
H300E	300	H	Elastomeric	140	120	540	7 × 7
Y400	400	inverted Y	Released	170	160	720	6 × 7
Y400E	400	inverted Y	Elastomeric	170	160	720	6 × 7
H400	400	H	Released	170	160	720	9 × 9
H400E	400	H	Elastomeric	170	160	720	9 × 9
Y500	500	inverted Y	Released	200	200	900	8 × 8
Y500E	500	inverted Y	Elastomeric	200	200	900	8 × 8
H500	500	H	Released	200	200	900	12 × 12
H500E	500	H	Elastomeric	200	200	900	12 × 12
Y400-RS	Pylon's stiffness and mass are half of Y400 and all other features are the same						

### Finite Element Models

All models were developed and analyzed using the CsiBridge software [10]. Decks consist of two main girders on each side and cross-girders connecting the two main girders at 6 m spacing. Width of the deck was 22 meters (see Figure 1). These girders were not modeled directly, instead a single frame element with equivalent stiffness was used for each span.

The decks in side-spans were heavier than the decks in main span, because a zero deflection under dead load was desired throughout the spans. The cables were prestressed in all models to obtain a straight horizontal deck after deformation of the bridge under the dead load. The 61 wire steel strand cables had an ultimate strength of 1740 MPa and yield strength of 1200 MPa. The structural steel used had a yield strength of 360 MPa. All pylon bases were considered as fixed. Connections between abutments at

the ends of the bridge and the deck were restricted in the transverse and vertical directions and for torsional rotation.

### Ground Motions for Time History Analyses

A suite of four-time history records, each consisting of two horizontal and one vertical component, were considered. The suite consisted of Imperial Valley (El Centro station), Tabas (Dayhook station), Northridge (Sylmar station), Loma Prieta (Corralitos station) and San Fernando (Pacoima dam station) records. The bridges were analyzed four times for each time history record. The first analysis used all three components of the record in which the strong horizontal component of earthquake was applied along the longitudinal direction. The second analysis was like the first one,

but the vertical component of the earthquake was eliminated. For the third analysis, the direction of the strong horizontal component was changed to be in the transverse direction of the bridge. In the last analysis, the vertical component was eliminated from the previous analysis. Both horizontal components of time history records were scaled to the AASHTO [11] design code spectrum shown in Figure 2. The nonlinear time history analyses using direct integration scheme were started after applying the dead loads on the structure. The two first main horizontal modes damping ratio was assumed as 2% and the Rayleigh damping modal matrix was formed by the program in accordance with mass and stiffness proportional damping rules.

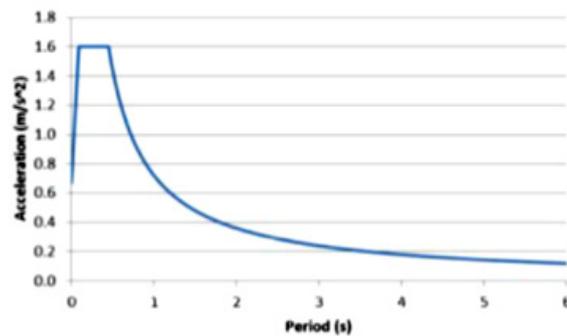


Figure 2: Design response spectrum of AASHTO.

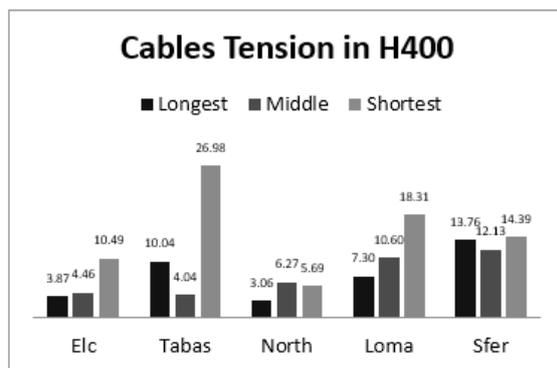
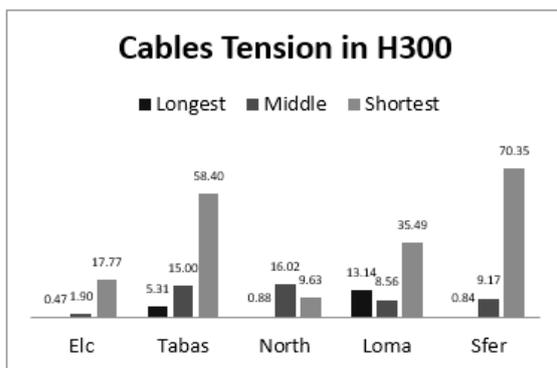
### Analyses Results

The effect of vertical component of earthquake on cable-stayed bridges was examined by comparing the difference in response of the bridge components resulting from three-components (3C) and two-components (2C) time history analyses. This comparison was evaluated as  $(3C-2C)/2C$  ratio which gives the percent difference of the internal force when vertical component is considered.

#### Cable Forces

The values for this ratio are plotted in Figure 3 for the longest, middle, and shortest stay cables of bridge models for the considered earthquake records. The shortest cables are near the pylons and are affected the most by the vertical component of the earthquake records. The figure shows the trend of decreasing ratio as the

length of cables increase. This trend is repeating in all bridges and earthquake records except in Northridge record in main span length of 300 meters and San Fernando record in main span length of 400 meters. These exceptions are related to frequency content of records and dynamic characteristic of bridges. These figures show that great errors can occur in analysis when the vertical component of the earthquake is ignored. For example, the cable tension ratio for San Fernando record for H300 model is as high as 70%. This means a 70% higher tension force is expected when the vertical component is considered in the analysis of this bridge. The results from Loma and San Fernando are intensified because of the vertical frequency content of these records which was close to the vertical periods of bridges.



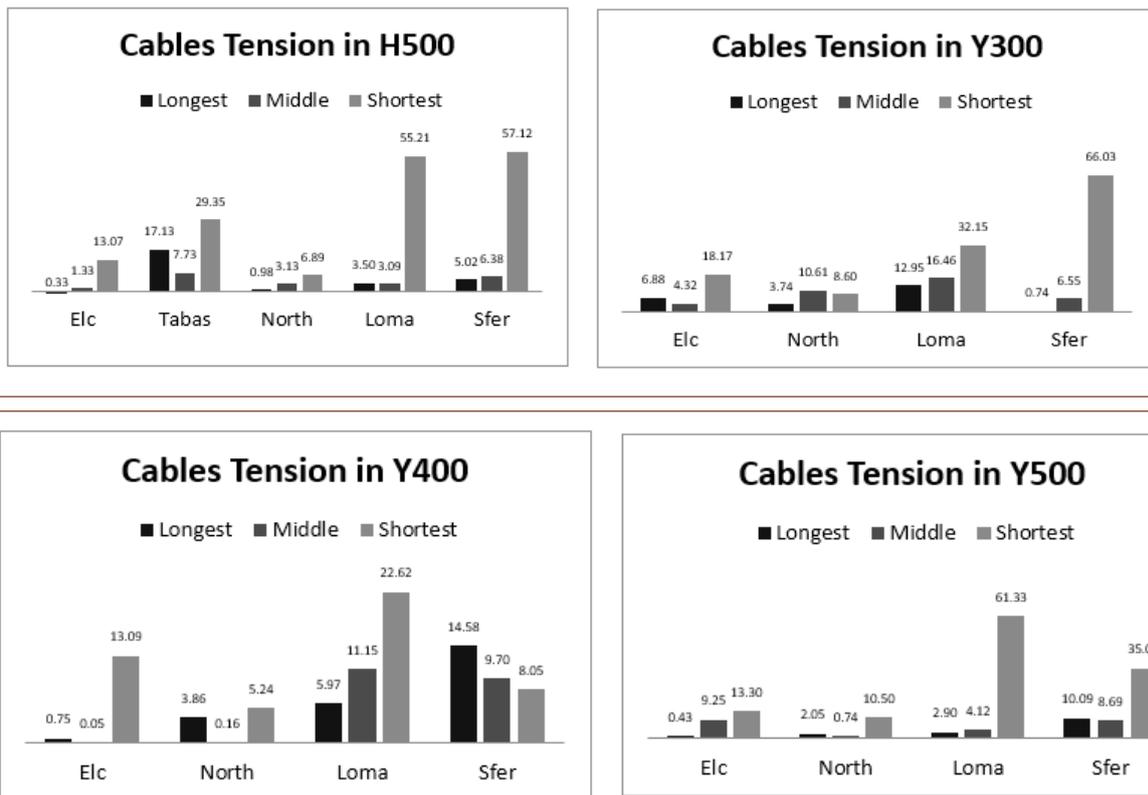


Figure 3: Percentage increase for cable forces due to vertical component.

### Deck Forces

In Table 3 the percentage increase for the deck forces and moments are displayed for selected bridges when vertical component is considered. The most significant force which is influenced by the vertical ground motion is the axial tension at midspan of the deck. This force fluctuates up to 101% if the vertical ground motion is considered (Loma earthquake in Y300). The

maximum compression force in the deck is located near the pylons and it seems that it is not very sensitive to the vertical component of earthquakes. The maximum positive moment in the deck occurred near the midspan and the (3C-2C)/2C ratios for this moment went up to 14% (Loma Y500). The maximum negative moments in the deck were not as significant as positive moments. However, in a special case (Loma Y300) it was increased to 23.61%.

Table 2: Bridge models dynamic characteristics.

Bridge Model	Fundamental periods (s) and [Mass Participation %]		
	Longitudinal	Transverse	Vertical
Y300	2.62 [53]	0.55 [63]	0.14 [42]
H300	2.38 [39]	1.53 [73]	0.15 [35]
Y400	3.4 [33]	0.65 [65]	0.16 [51]
H400	2.95 [24]	1.75 [27]	0.15 [43]
Y500	4.04 [31]	2.92 [10]	0.22 [21]
H500	3.61 [24]	1.85 [40]	0.21 [43]
Y400-RS	3.25 [27]	0.71 [18]	0.16 [18]

Table 3: Percentage increase for the deck forces.

Bridge Model	Earthquake Records	Compression	Tension	Negative Moment	Positive Moment
H300	Elcentro	0.62	17.59	2.63	0.45
	Loma	12	66.2	5.04	0.62
	Northridge	0.55	5	0.72	3.11
	SanFernando	1.1	5.48	2.97	5.4

Y300	Elcentro	1.55	5.6	1.03	1.98
	Loma	14.76	101	23.61	2.25
	Northridge	4.78	3.3	0.93	3.75
	SanFernando	2.95	3.99	3.56	1.55
H400	Elcentro	0.83	5.18	0.4	0.61
	Loma	0.42	49.41	1.87	1.84
	Northridge	2.21	3.14	1.61	2.57
	SanFernando	0.18	2.16	9.15	7.83
Y400	Elcentro	6.12	19.23	1.64	3.71
	Loma	8.53	71.81	4.93	7.58
	Northridge	4.45	6.48	0.9	0.39
	SanFernando	5.38	4.68	7.53	1.69
H500	Elcentro	4.21	2.63	3.7	3.98
	Loma	5.13	4.36	6.3	8.8
	Northridge	1.02	1.89	1	0.52
	SanFernando	9.5	4.04	2.38	12.92
Y500	Elcentro	1.06	8.3	9.12	0.33
	Loma	2.83	28.89	11.25	13.93
	Northridge	0.63	8.66	0.6	3.16
	SanFernando	2.6	4.85	1.63	10.26

### Other Forces

In addition, some other internal forces and displacements were monitored to examine the error resulting from eliminating the vertical component of ground motions. These were deck weak

axis moment, deck torsion, deck transverse shear and horizontal displacements of pylons top. These features were not affected significantly (below 15%) by the vertical component and are not shown for brevity.

**Table 4:** Percentage increase in pylon forces.

Bridge Model	Earthquake Records	Axial		Moment
		Compression	Tension	
H300	Elcentro	6	3	1
	Loma	20	6	1
	Northridge	36	48	8
	SanFernando	78	38	3
Y300	Elcentro	34	144	2
	Loma	42	74	3
	Northridge	35	61	3
	SanFernando	147	184	4
H400	Elcentro	21	4	4
	Loma	49	6	5
	Northridge	45	2	7
	SanFernando	31	20	9
Y400	Elcentro	73	4	1
	Loma	36	17	5
	Northridge	18	11	1
	SanFernando	66	16	3

H500	Elcentro	22	24	3
	Loma	27	15	6
	Northridge	47	1	8
	SanFernando	127	20	10
Y500	Elcentro	14	7	0
	Loma	143	88	0
	Northridge	143	6	0
	SanFernando	161	18	1

**Pylon Forces**

Table 4 shows the (3C-2C)/2C ratio at the base of pylons. As the table indicate the moment in the pylons were not sensitive to the vertical earthquake components and the ratios for moments were below 10%. The crucial forces in pylons were tension and compression axial forces. The increase in these forces depend on

bridge span and frequency content of earthquakes, but as a rule of thumb, as the main span of bridges was increased the ratios increased. In addition, the inverted Y pylon could be influenced more significantly by the effect of vertical component of earthquakes than bridges with H pylon.

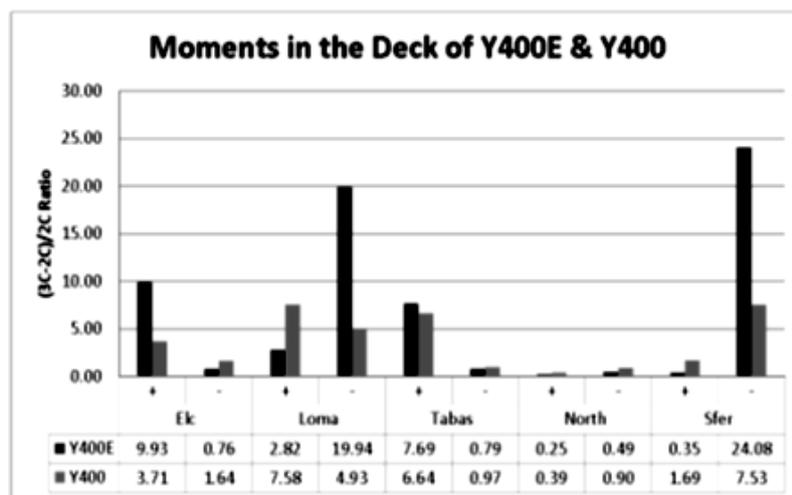
**Table 5:** Percentage increase of forces for deck due to deck-pylon connection.

Bridge Model	Earthquake Records	Moments	Axial Tension	Axial Compression
Y400 With Longitudinal Connection	San Fernando	7.53	4.68	5.38
Y400 Without Longitudinal Connection	San Fernando	10.35	19.78	11.11

**Effect of deck-pylon connection**

As mentioned previously, bridges were analyzed for two types of deck-pylon connection. In the first type the vertical support at pylon was eliminated and the bridge was hanging from the cables. In the second type (Type E), an elastomeric bearing was provided at the deck/pylon connection. Overall, the first type was more

sensitive to vertical component of the earthquake. The effect of this parameter on the positive and negative moments in the deck is illustrated in Figure 4. A maximum of 24% increase in moments can occur when vertical component is considered in the analyses. Figure 5 shows the worst increase in axial deck forces which is as high as 118%. Figure 6 shows the worst increase in deck shear forces which is as high as 26.5%.



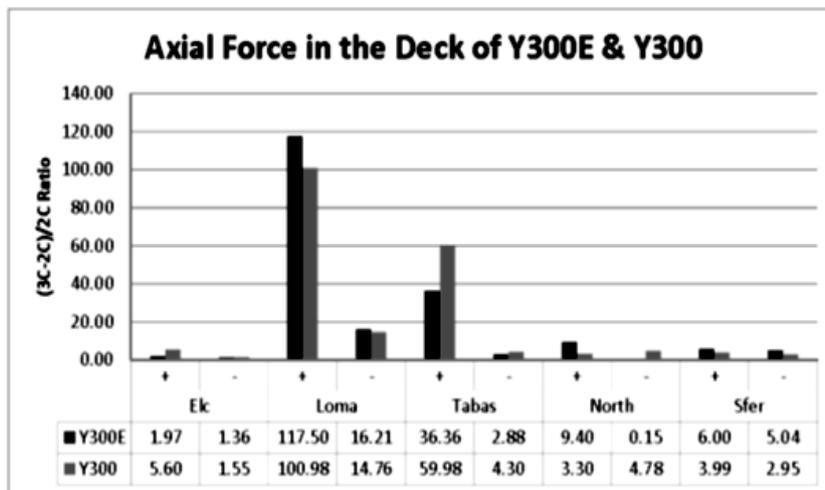
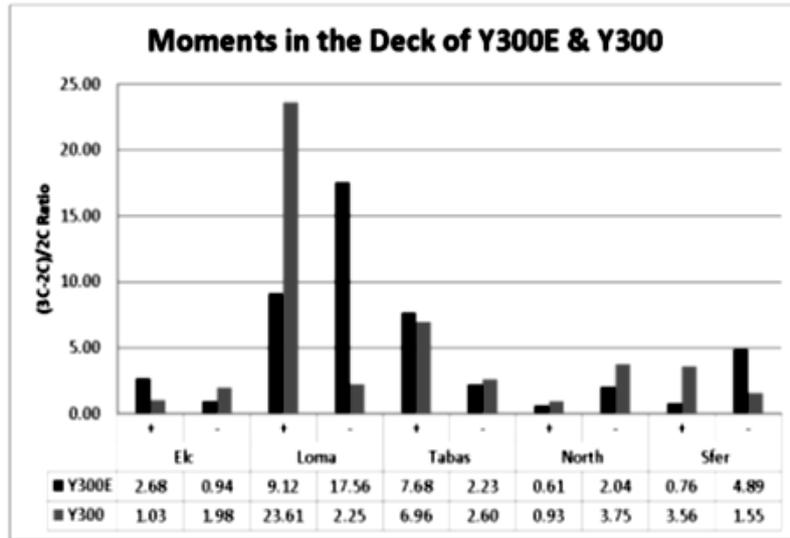


Figure 4: Deck moment in bridges with no vertical support vs. elastomeric support (Type E).

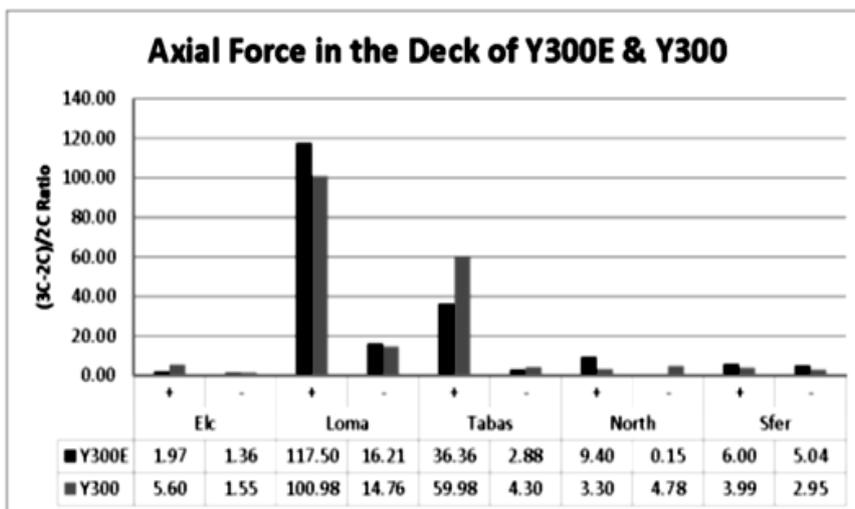


Figure 5: Deck axial forces in bridges with no vertical support vs. elastomeric support (Type E).

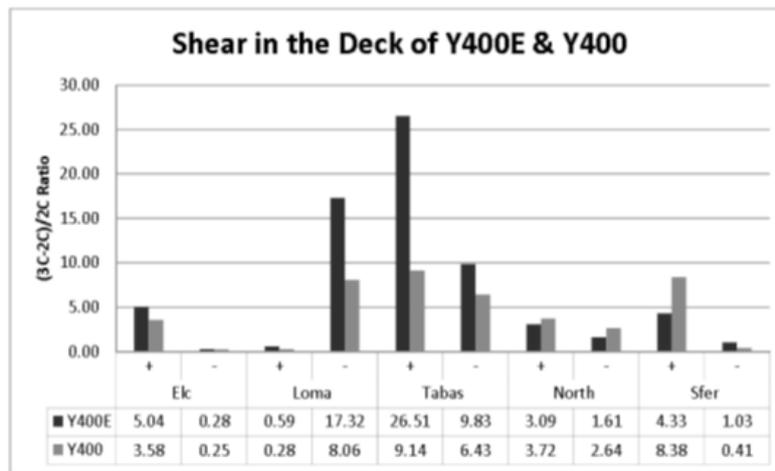


Figure 6: Deck shear forces in bridges with no vertical support vs. elastomeric support (Type E).

In another model, the effect of eliminating the longitudinal connection of deck-pylon was investigated. The results as shown in Table 5 shows that, the  $(3C-2C)/2C$  ratios in cables increased when the decks were not connected to pylons longitudinally. In addition, the ratios for deck forces were increased. Moreover, the forces in pylons were decreased.

### Effect of Pylons Stiffness

The stiffness used in analyses of bridges was calculated by the program. To examine the sensitivity of vertical response to this parameter, time history analyses were performed on Y400 bridge using moment of inertia and cross-sectional area and masses that were halved. This model is called Y400-RS. The dynamic

Table 6: Percentage increase of pylon forces due to reduced stiffness.

Model	Earthquake Records	Axial Tension	Positive Moment
Y400	Elcentro	16.16	2.93
	San Fernando	4.68	1.73
Y400-RS	Elcentro	49.63	3.1
	San Fernando	38.89	2.66

### Effect of pylon type

Vertical component of earthquakes affected the bridges in both pylon types. In the deck, the inverted Y pylons generate greater difference in forces than H pylons when vertical component was considered. In addition, the inverted Y pylons were affected more significantly in axial tension and compression forces in the pylons. Figure 7 shows a maximum of 14% increase in Y-500 in comparison to H-500 bridge models.

### Conclusion

Bridge design codes like AASHTO have not provided specific vertical response spectra for the design of bridges. This research, by using extensive nonlinear time history analyses on selected bridges, showed that the effect of vertical component of earthquakes on the

characteristic of the bridge was not changed significantly, for the mass and the stiffness of the pylons change simultaneously and the period of the whole structure was almost the same. Table 6 shows the level of forces in both bridges. The level of forces in reduced stiffness bridge is decreased significant; as a result, the designing of the pylons could be very important in forces in deck.

The  $(3C-2C)/2C$  ratios in both of bridges for San Fernando earthquake are shown in Table 6. As the table shows, the ratio in RS bridge is higher especially, in maximum tension forces of the deck. However, the  $(3C-2C)/2C$  ratios for cable forces were the opposite. Also, displacement in the middle of the deck increased significantly as the stiffness of the pylons was reduced.

cable-stayed bridges considered can be very significant in some cases.

The conclusions for this study are as follows:

1. The impact of vertical ground motion is significant and cannot be ignored.
2. The cable forces near the pylons showed a maximum increase of 70% when the vertical component of earthquake was considered.
3. The axial tension at the midspan of the deck showed a maximum increase of 100% when the vertical component of earthquake was considered.

4. The deck weak axis moment, deck torsion, deck transverse shear and horizontal displacements of pylons were not affected significantly when the vertical component of earthquake was considered.
5. The inverted Y pylons were affected more by the vertical earthquake than the H pylon cable-stayed bridges.
6. Having a vertical support at the deck-pylon connection

was better than not having a vertical support.

7. As the pylons stiffness and mass were decreased by 50%, the level of deck forces was increased significantly.
8. The responses showed that releasing the longitudinal restraint at the deck/pylon connection increased the cable forces and deck forces. However, the forces in pylons were decreased.

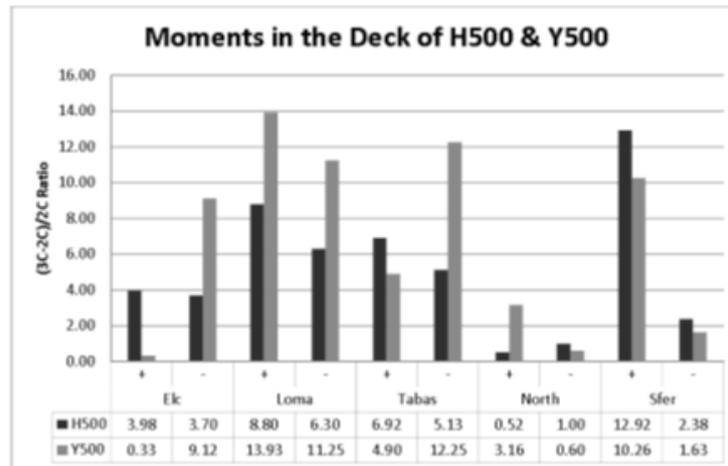


Figure 7: Deck moments (+/-) in bridges with different pylon types.

## Acknowledgement

None.

## Conflict of Interest

No conflict of interest.

## References

1. Saadeghvaziri MA, Foutch DA (1991) Dynamic behavior of R/C highway bridges under the combined effect of vertical and horizontal earthquake motions. *Earthquake Engineering and Structural Dynamics* 20: 535-549.
2. Yu CP, Broekhuizen DS, Roeset JM, Breen JE, Kreger ME (1997) Effect of vertical ground motion on bridge deck response. Proc., Workshop on Earthquake Engineering Frontiers in Transportation Facilities, Tech. Rep. No. NCEER-97-0005, National Center for Earthquake Engineering Research, State Univ of New York at Buffalo, N.Y.: 249-263.
3. Button MR, Cronin CJ, Mayes RL (2002) Effect of Vertical Motion on Seismic Response of Highway Bridges. *ASCE Journal of Structural Engineering* 128: 1551-1564.
4. Gloyd S (1997) Design of ordinary bridges for vertical seismic acceleration. Proc., FHWA/NCEER Workshop on the National Representation of Seismic Ground Motion for New and Existing Highway Facilities, Tech. Rep. No. NCEER-97-0010, National Center for Earthquake Engineering Research, State Univ of New York at Buffalo, N.Y.: 277-290.
5. Elnashai AS, Papazoglou AJ (1997) Procedure and spectra for analysis of RC structures subjected to strong vertical earthquake loads. *J Earthquake Eng 1(1)*: 121-155.
6. Collier CJ, Elnashai AS (2001) A Procedure for Combining Vertical and Horizontal Seismic Action Effects. *Journal of Earthquake Engineering* 5(4): 521-539.
7. Veletzis MJ, Restrepo JI, Seible F (2006) Seismic response of precast segmental bridge superstructures. Cal Trans Tech. Report UCSD/SSRP-06/18.
8. Abdel Ghaffar AM, Nazmy A (1991) Nonlinear Seismic Behavior of Cable-Stayed Bridges. *Journal of Structural Engineering* 117(11).
9. Shrestha B (2015) Seismic response of long span cable-stayed bridge to near-fault vertical ground motions. *KSCE Journal of Civil Engineering* 19: 180-187.
10. AASHTO (2020) LRFD bridge design specifications (9th ed.). The American Association of State Highway and Transportation Officials.
11. CsiBridge, version 20, Computers & Structures, Inc. Structural and Earthquake Structural Software. California, USA.